

Micro-Grid Droop Control Strategy and Isolated Island Operation System Stability Analysis

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Abstract: -In the micro-grid, droop control strategy simulates traditional power system droop characteristics , by changing the output of active and reactive power to control the output voltage frequency and amplitude, thus the micro-grid system can work at the stabilize voltage point in island operation mode . And the voltage is more or less with the grid-connect mode,so that the transition is smooth when switching,which can guarantee the load work undisturbed. Microgrid based on droop control can achieve automatically adjust voltage and frequency, without the aid of communication, which can improve system reliability, and easy to implement micro-power and load plug and play. We designed specifically simulation circuit for the droop control strategy on PSIM . And the output waveform is studied. Simulation results show the schematic design of the control strategy is correct.We established an island microgrid complete small-signal state space model, which took into account the inverter power small-signal sub-model, network lines and the load small signal sub-model.It use eigenvalue method to analysis microgrid small signal model state matrix, to get the following conclusions: droop coefficient increases will reduce the stability of the micro-grid system; when the line impedance is smaller, micro-grid is easy to lose stability. Finally, We use the simulation tools to verify the small signal stability analysis conclusions is correct.

Key-Words: - microgrid, droop control, PSIM, Simulink, converter, small signal stability analysis

1 Introduction

Today's power system development has already closely integrated with modern control theory. Power grid is developing toward two distinct directions: a large capacity, long-distance, high pressure, even UHV AC and DC transmission level and a large grid interconnection; the other is small capacity and relatively independent micro-grid. For these two directions, there are still some common problems (such as the optimization of operation, coordinated scheduling and control, etc.) to be resolved. Over the past decades, power grid develops rapidly ,and now has become a major power transmission channel. But with the power grid scale up and the whole society deepen the dependence on electricity, the drawbacks of ultra-large-scale systems are also reflected, such as high cost, difficult to run and so on. In addition, worldwide energy supply remains tense, it is imminent to rationally develop and utilize new energy. Distributed generation with the installation location flexibility and high efficiency of energy use, can effectively solute many problems of large

centralized power grid. Therefore, distributed generation was put on the agenda. Distributed power has obvious advantages, there are also some problems, such as high-cost to access to distributed power, difficult to control. Moreover, for a large grid, distributed power source is not controllable. The system often take quarantine and restriction approaches to DG, to reduce the impact on the grid. In addition, IEEE1547 provides DG network standard, that is, if the system fails, the distributed power must be immediately quitted running. This leads to distributed power can not be fully effectived. Scholars in order to coordinate the contradiction between DG and large grid, put forward the concept of micro-grid.

Micro grid (MG) can be combined with the loads, generators, control devices and energy storage devices into a manageable unit, with a lot of non-linear distributed power. It can not only solve the problem of large-scale distributed power access, but also bring the user and the system many benefits. Thus microgrid research is useful supplement of the existing backbone network .It is

of great significance whether for the use of new energy from the environmental point of view, or considering increasing the supply of quality and reliability of power supply from the backdrop of China's power grid interconnection . Among them, one of the key problems of the study of micro-grid is coordination and control technology and energy management systems research.

In summary, micro network converter control method study has great significance and application prospects.

2 Micro-Grid Inverter Control

Micro-network (MG) has a variety of different types of distributed power (DG) and extensive power electronic devices to interconnect, resulting in the existence of a fundamental difference between micro-grid and general transmission and distribution systems; In addition, because of micro-grid system can run on-grid and can run off-grid operation mode. It need to switch. It also brings many complex control problems. That must take control methods different from the traditional methods, or make a large adjustment.

For parallel operation of DG, the main control methods are several programs such as non-contact line control based on droop, master-slave control, centralized control and decentralized logic control. Last three options need contact line to communication. In distributed generation systems, each power supply spacing stays away. The transmission signal is complex, reducing system reliability. No tie-line control scheme is that droop control based on local electrical quantities to adjusted DG . It can respond MG dynamic process in a very short period of time, to meet the requirements of real-time control.

3 Droop Control Strategy

3.1 Droop Control Method Operating Principle

Droop control is in essence the voltage source inverter voltage-controlled method , by adjusting the voltage amplitude and phase to achieve control of the transmission power. In the inductive transmission line, active power mainly depends on the power angle. Reactive power depends on the voltage difference. So Power angle can be used to

control active power and voltage difference can be used to control reactive power.

In the micro-grid, the droop control strategy simulates the droop characteristics of traditional power system, by changing the output of active and reactive power to control the frequency and amplitude of the output voltage, so that micro-grid system can work on stabilize voltage point in island operation mode . And it is less different with the network mode voltage. Transition is smooth when switching, that can guarantee the load undisturbed to normally work. The figure below shows the frequency - the active and voltage - reactive droop curve.

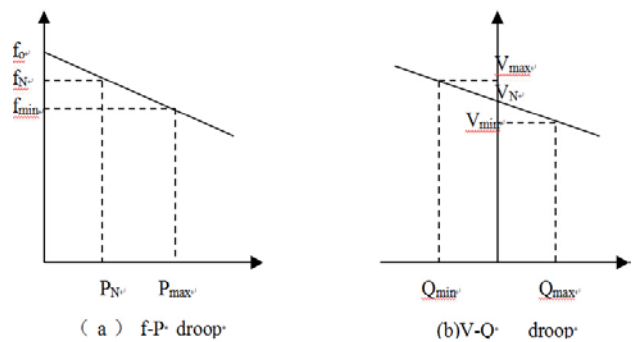


Figure 1. drooping curve:(a) f – P droop (b) V-Q droop

Wherein the f_0 is no-load frequency. The f_N is the nominal frequency. The f_{min} is minimum frequency for the power quality permission. The P_N is nominal active power output. The P_{max} is maximum power output. The V_{max} , V_{min} is the maximum and minimum voltage of the system. The V_N is rated voltage. The Q_{min} , Q_{max} is the minimum and maximum output reactive power.

The control strategy: To get the output current and voltage by current and voltage sensors detecting. Then the micro-power active and reactive power output is calculated at this time to obtain voltage frequency and amplitude reference values in accordance with the droop curve setting, and then to control the inverter output current and voltage. Entire droop control system consists of the power calculate unit, droop control unit, voltage and current double closed loop control unit and modulation unit and other units, as shown below.

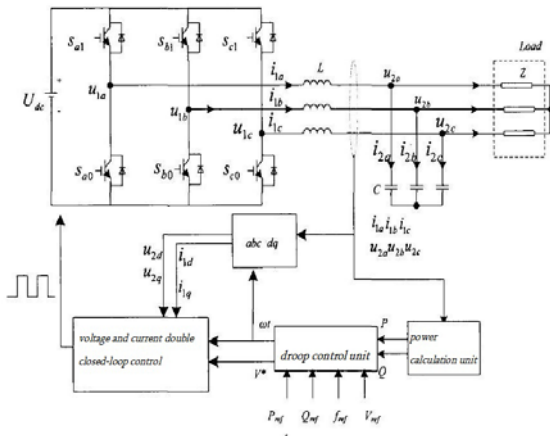


Figure 2. drooping curve droop control chart

3.1.1 Power Calculation Unit

First transform three-phase AC voltage and current detected by sensors by Parker to two-phase DC voltage and current, with two-phase DC quantities to represent the three-phase AC quantities, can make computing easier, and is good to the inverter output astatic regulation.

3.1.2 Droop Control Unit

Droop control unit is a core unit of distributed power droop control. Enter the active and reactive power issued by inverter. Output reference value of the voltage amplitude and phase angle ωt . Previously given frequency droop and voltage sag slope m and n , by calculating the output power of the inverter determine the voltage amplitude and frequency output of distributed power at this time. Calculate the voltage and frequency reference value in accordance with the graphics this time.

$$f = f_N + m(P_N - P) \tag{1}$$

$$V = n(Q_N - Q) \tag{2}$$

The f_N is the nominal frequency, typically 50Hz. The P_N and Q_N stand for inverter rated active power and reactive power. The Q_N usually sets to 0. The P, Q stand for the previous unit input active and reactive power. The f, V are the frequency and voltage amplitude reference value. The m, n are the frequency and voltage droop coefficient.

After obtained the frequency reference value f , by integrating operations, and then multiply 2π can get the phase angle reference value ωt .

$$2\pi f = \omega = \frac{d\delta}{dt} \tag{3}$$

3.1.3 Voltage and Current Double Closed-Loop Control

Voltage and current double closed-loop control unit is also droop control strategy important aspect, in which the outer ring is the voltage closed-loop. The inner loop is the current loop. The current loop control is mainly to improve the dynamic response of the system. The outer loop voltage control is mainly to eliminate the system steady-state error, for the output of distributed power better tracking presets. To obtain the voltage amplitude and phase angle reference value then can generated a three-phase modulated wave signal. Before comparing with the triangular carrier, it need to get through a voltage and current double closed-loop control unit, to achieve the output waveform astatic control. First convert three-phase sine wave signal to dq two-phase signal. Respectively Calculate the difference with the sensor detects the output voltage U_d, U_q , and the output current i_d, i_q . Then get through the proportional regulator. And finally converted back to a three-phase AC quantities to become modulated wave signal.

3.1.4 Modulation Unit

Three-phase AC modulation wave signal is compared with the triangular carrier signal. When the modulation signal is greater than the carrier signal, control IGBT conduction. When the modulation signal is less than the carrier signal, control IGBT turn-off. That can get output voltage SPWM waveform, then filter out high harmonics by the low-pass filter, and ultimately get the three-phase sinusoidal voltage waveform.

When micro-grid uses the droop control strategies, the micro-powers do not require to contact with each other, as long as detecting local output voltage and current size, then according to the principle of droop control to obtain the output voltage frequency and amplitude reference value. It is for peer control between the system micro power. When the rated capacity of micro-power is unequal, each micro power voltage, frequency droop coefficients can be separately calculated based on the rated capacity. To make all micro-power droop coefficients and the rated power's product is equal, as the following equation. This allows the system micro-power according to their rated capacity to distribute reasonable loads. That will not cause a micro power underutilized or overload damage.

Wherein the S_1, S_2, \dots, S_n are for each distributed power rated capacity. The m_1, m_2, \dots

are each distributed active power droop curves slope. The n_1, n_2, \dots are each distributed active power droop curves slope.

3.2 Build Simulation Models

3.2.1 Droop Control Unit

Set the rated voltage amplitude 311V and rated frequency 50Hz. Set rated active power and reactive power 4000 and 2000 respectively. Active and reactive droop coefficient are 0.0005 and 0.01 respectively. Generated phase δ is as other aspects ωt input.

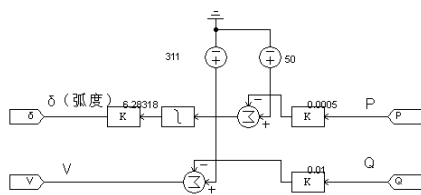


Figure 3. droop control unit

3.2.2 Generates Three-Phase Modulation Wave Signal with the Voltage Amplitude and Phase Angle Reference Value

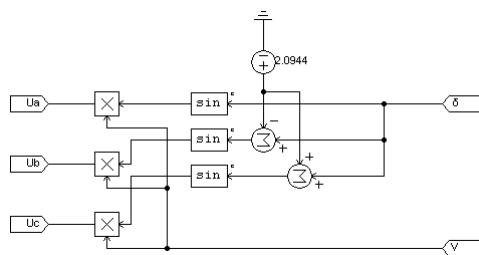


Figure 4. modulation wave signal generating unit
A phase angle is ωt . B is with a phase lag 2.0944 radians. C phase is ahead of A phase 2.0944 radians. Then convert the three-phase alternating current signal back to two-phase DC signal.

3.2.3 Power Calculation Unit voltage and current double closed-loop control

$$m_1 \times S_1 = m_2 \times S_2 = \dots = m_n \times S_n \quad (4)$$

$$n_1 \times S_1 = n_2 \times S_2 = \dots = n_n \times S_n \quad (5)$$

The voltage source control is the outer loop. The proportional source controller gain is 0.3. The current

source control is inner loop, The proportional regulator gain is 3. After the voltage and current double closed-loop control, then converting dq two-phase signal back to abc three-phase signal, the signal can be obtained as the modulation wave signal, involved in generating a PWM waveform.

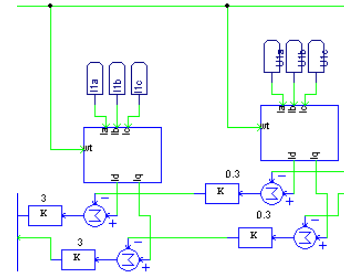


Figure 5. dual-loop control

3.2.4 Modulation Aspects

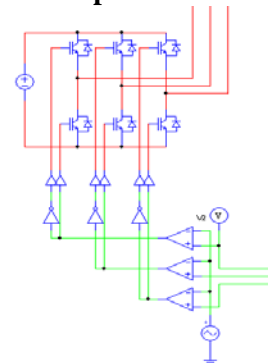


Figure 6. modulation unit

Triangular wave generator parameters: peak voltage is 800V. Frequency is 7000Hz. DC offset is -400V. DC voltage source is 800V.

3.2.5 The Entire Droop Control Simulation Circuit

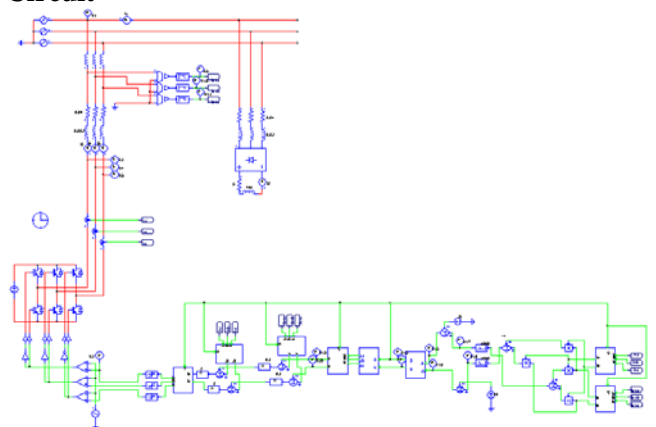


Figure 7. Droop control diagram

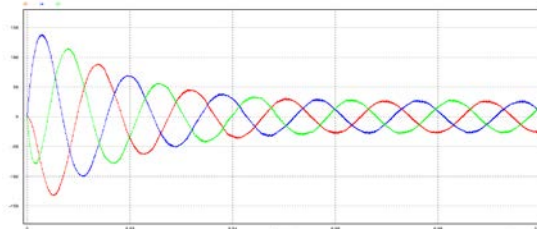
The line reactance is much larger than the resistance parameters. The load is DC load after three-phase

bridge rectifier circuit . Voltage sensor measured current through the low-pass filter cut-off frequency is 1000Hz. Power calculation unit output active and reactive power also need to go through the filtering effect. The cutoff frequency is setted to 1000Hz. Modulation wave signal need enter a restrictor before through a comparator, limiting the amplitude of the waveform. The parameter is setted from -400V to +400V.

3.3 Simulation results

Triangular wave generator parameters: peak voltage is 800V. Frequency is 7000Hz. DC offset is -400V. DC voltage source is 800V.

1) Inverter output three-phase current and voltage are shown in figure below, showing the output current stabilized after 0.04 seconds, and control is the rapid.



(a) output current



(b) output voltage

Figure 8. (a) output current (b) output voltage
Output voltage after low-pass filter is as shown.

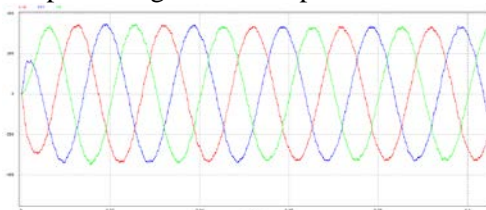


Figure 9. low-pass filter output voltage

2) Output voltage amplitude:

$$U_m^2 = U_\alpha^2 + U_\beta^2 \tag{6}$$

It is consistent with figure the output voltage waveform magnitude.



Figure 10. Output voltage amplitude
3) output active power and reactive power:

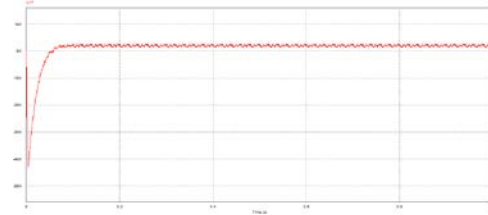


Figure 11. Output active power

Active power stabilized at about 2kW, and is less different with values calculated by the inverter output voltage and current.

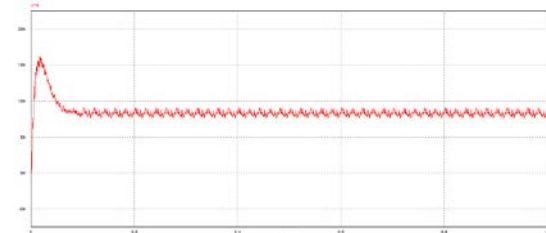


Figure 12. reactive power output

Reactive power is about 7kVar

4) voltage magnitude and phase angle reference value:

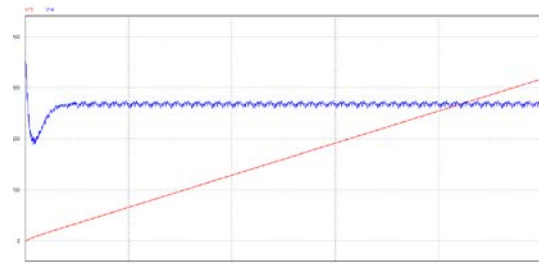


Figure 13. voltage amplitude and phase angle

Level curve is voltage amplitude pattern. Tilt curves is angle graphics. The voltage amplitude reference value is about 270V. The slope of the curve of the phase angle curve is approximately 317.08. That can calculate at this time frequency reference value is 50.46Hz .

4 Islands Microgrid Small Signal Stability Analysis

Compared with the large grid, microgrid capacity is generally small. The system inertia with respect to the bulk power system inertia can even be negligible. Therefore when micro power grid operation with grid, dynamic process and stability of the system depends on the power grid; And when islanding operation, the stability of the microgrid depends on its own control part and network structure, susceptible to disturbances and loss of stability. One of the important conditions for safe and stable operation of the microgrid under islanding state is able to maintain its small signal stability. The time

constant of large power rotation generators and control systems is much larger than the time constant of the network, so the network and load can use no dynamic equivalent impedance model. The traditional power systems small signal stability analysis often neglects network dynamics characteristics impact. In the small signal stability analysis of the micro-grid, due to the micro-power mostly through the very short response time power electronic inverter access, dynamic characteristics of the network will affect the stability of the system.

In this paper, the establishment of microgrid islands small-signal model fully consider the impact of network dynamics. It establish inverter control system small-signal sub-model and the network line small-signal sub-model considering the dynamic characteristics and load small-signal sub-models. These sub-models are established at their rotating coordinate system. Through coordinate transformation, all the sub-models are converted into a unified reference coordinate system and combined to establish a complete micro-grid small-signal state space model, to get the system state matrix , to analysis stability caused by the parameters change by characteristic value method.

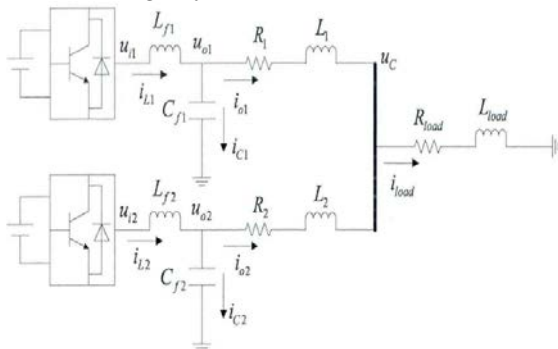


Figure 14 islands microgrid simplified equivalent circuit

Microgrid island operation equivalent circuit is shown in Figure 14. To simplify the analysis, it only consider connected to the micro-grid AC bus variable load, and filter inductor current is for a state variable , filter capacitor current can be represented by filter inductor current and output current .

4.1 Coordinates Transformation

In this paper, the study subject Microgrid comprises two inverter-based micro sources, and the small-signal model for each inverter is built on the dq rotating coordinate system determined by its outlet voltage, with the rotation frequency confirmed by the corresponding power controlling unit. Dq rotating coordinate systems are different for different inverters. In order to establish the whole

micro-grid small signal model, all the models need to be converted to a unified reference coordinate system through coordinate transformation. We Select one inverter dq rotating coordinate system as a common reference coordinate system DQ. And another small-signal model inverter power rotating coordinate system needs convert to this common reference coordinate system.

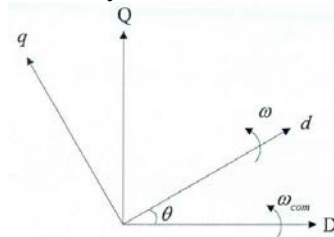


Figure 15 coordinate systems transformation

The coordinate systems transform relationship is shown in Figure 15. ω_{com} is the angular frequency of the common reference coordinate system. ω is the angular frequency of another rotating coordinate system. θ is for different rotating coordinate system d axis phase difference. Coordinate conversion formula is:

$$f_{DQ} = T f_{dq} \tag{7}$$

The corresponding inverse transform formula is as follows:

$$f_{dq} = T^{-1} f_{DQ} \tag{8}$$

$$T = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}, T^{-1} = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$$

4.2 Inverter Parallel System Small Signal Model

4.2.1 Power Controller Small Signal Model

Shown in Figure 15, θ can be expressed by

$$\theta = \int (\omega - \omega_{com}) dt \tag{9}$$

Inverter power output three-phase AC voltage and current transformed into a dq rotating coordinate system DC quantity through Park transformation. And thus the instantaneous active power, reactive power can be calculated as follows:

$$p = u_{od} i_{od} + u_{oq} i_{oq} \tag{10}$$

$$q = u_{od} i_{oq} - u_{oq} i_{od} \tag{11}$$

To minimize the effects of harmonics, the instantaneous active power p, reactive power q need low-pass filter to obtain the droop control required active power P and reactive power Q.

$$P = \frac{\omega_c}{s + \omega_c} p \quad (12)$$

$$Q = \frac{\omega_c}{s + \omega_c} q \quad (13)$$

ω_c is the low-pass filter corner frequency. s is the Laplace transform factor.

Power controller droop characteristic equation can be written as follows:

$$\omega = \omega_n + m_p (P_n - P) \quad (14)$$

$$U = U_o - nQ \quad (15)$$

ω_n is the nominal angular frequency of micro grid. U_o is microgrid rated voltage. $m_p = 2\pi m$. m is for active power droop factor. n is for reactive power droop factor.

By considering the formulas (9)to(15), and linearising above all, we can get power controller small signal state-space model:

$$\begin{bmatrix} \Delta \dot{\theta} \\ \Delta \dot{P} \\ \Delta \dot{Q} \end{bmatrix} = A_p \begin{bmatrix} \Delta \theta \\ \Delta P \\ \Delta Q \end{bmatrix} + B_p \begin{bmatrix} \Delta i_{ldq} \\ \Delta u_{odq} \\ \Delta i_{odq} \end{bmatrix} + B_{p\omega} \Delta \omega_{com} \quad (16)$$

$$\begin{bmatrix} \Delta \omega \\ \Delta u_{odq} \end{bmatrix} = \begin{bmatrix} C_{p\omega} \\ C_{pu} \end{bmatrix} \begin{bmatrix} \Delta \theta \\ \Delta P \\ \Delta Q \end{bmatrix} \quad (17)$$

Δi_{ldq} , Δu_{odq} , Δi_{odq} and Δu_{odq}^* are vectors, such as $\Delta i_{ldq} = [\Delta i_{ld} \ \Delta i_{lq}]^T$. Vector representation elsewhere in the text is similar with here. $\Delta \omega_{com}$ is the common reference coordinate system angular frequency deviator. Coefficient matrixs are respectively:

$$A_p = \begin{bmatrix} 0 & -m_p & 0 \\ 0 & -\omega_c & 0 \\ 0 & 0 & -\omega_c \end{bmatrix}$$

$$B_p = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & \omega_c I_{od} & \omega_c I_{oq} & \omega_c U_{od} & \omega_c U_{oq} \\ 0 & 0 & -\omega_c I_{oq} & \omega_c I_{od} & \omega_c U_{oq} & -\omega_c U_{od} \end{bmatrix}, \quad B_{p\omega} = \begin{bmatrix} -1 \\ 0 \\ 0 \end{bmatrix}$$

$$C_{p\omega} = \begin{bmatrix} 0 & -m_p & 0 \end{bmatrix}, \quad C_{pu} = \begin{bmatrix} 0 & 0 & -n \\ 0 & 0 & 0 \end{bmatrix},$$

U_{od} , U_{oq} , I_{od} , I_{oq} are the initial steady-state operation parameters, similar to other such variables appear below.

4.2.2 Voltage and Current Double Loop Controller Small Signal Model

According to the design of voltage and current double loop controller, voltage outer control link mathematical expressions can be represented by the following formula:

$$\begin{cases} \dot{i}_{ld}^* = i_{od}^* - \omega C_f u_{oq}^* + K_{up}(u_{od}^* - u_{od}) + K_{ui} \int (u_{od}^* - u_{od}) dt \\ \dot{i}_{lq}^* = i_{oq}^* - \omega C_f u_{od}^* + K_{up}(u_{oq}^* - u_{oq}) + K_{ui} \int (u_{oq}^* - u_{oq}) dt \end{cases} \quad (18)$$

To simplify the analysis of voltage outer control link, we introduce state variables ψ_d and ψ_q to meet:

$$\begin{cases} \frac{d\psi_d}{dt} = u_{od}^* - u_{od} \\ \frac{d\psi_q}{dt} = u_{oq}^* - u_{oq} \end{cases} \quad (19)$$

Formula (18) and (19) were linearized to get voltage outer control link small-signal state space model:

$$\Delta \dot{\psi}_{dq} = [0] \Delta \psi_{dq} + B_{u1} \Delta u_{odq}^* + B_{u2} \begin{bmatrix} \Delta i_{ldq} \\ \Delta u_{odq} \\ \Delta i_{odq} \end{bmatrix} \quad (20)$$

$$\Delta i_{ldq}^* = C_u \Delta \psi_{dq} + D_{u1} \Delta u_{odq}^* + D_{u2} \begin{bmatrix} \Delta i_{ldq} \\ \Delta u_{odq} \\ \Delta i_{odq} \end{bmatrix} \quad (21)$$

Wherein the coefficient matrix are

$$B_{u1} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, \quad B_{u2} = \begin{bmatrix} 0 & 0 & -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \end{bmatrix}$$

$$C_u = \begin{bmatrix} K_{ui} & 0 \\ 0 & K_{ui} \end{bmatrix}, \quad D_{u1} = \begin{bmatrix} K_{up} & -\omega C_f \\ \omega C_f & K_{up} \end{bmatrix},$$

$$D_{u2} = \begin{bmatrix} 0 & 0 & -K_{up} & 0 & 1 & 0 \\ 0 & 0 & 0 & -K_{up} & 0 & 1 \end{bmatrix}$$

Similarly, the introduction of state variables λ_d and λ_q meets $\frac{d\lambda_d}{dt} = i_{ld}^* - i_{ld}$ can $\frac{d\lambda_q}{dt} = i_{lq}^* - i_{lq}$, to get the current inner control link small-signal state space model:

$$\Delta \dot{\lambda}_{dq} = [0] \Delta \lambda_{dq} + B_{i1} \Delta i_{ldq}^* + B_{i2} \begin{bmatrix} \Delta i_{ldq} \\ \Delta u_{odq} \\ \Delta i_{odq} \end{bmatrix} \quad (22)$$

$$\Delta u_{idq} = C_i \Delta \lambda_{dq} + D_{i1} \Delta i_{ldq}^* + D_{i2} \begin{bmatrix} \Delta i_{ldq} \\ \Delta u_{odq} \\ \Delta i_{odq} \end{bmatrix} \quad (23)$$

The coefficient matrix formula is as follows:

$$B_{i1} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, \quad B_{i2} = \begin{bmatrix} -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$C_i = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}, \quad D_{i1} = \begin{bmatrix} K & 0 \\ 0 & K \end{bmatrix}, \quad D_{i2} = \begin{bmatrix} -K & -\omega L_f & 0 & 0 & 0 & 0 \\ \omega L_f & -K & 0 & 0 & 0 & 0 \end{bmatrix}$$

4.2.3 Output Filters and Network Small-Signal Model

Inverter powers via the output LC filter access to micro-grid AC bus line. Filter inductor current i_i , inverter power output voltage u_o and output current i_o meet the following differential algebra equation:

$$\begin{cases} L_f \frac{di_{id}}{dt} = u_{id} - u_{od} - R_f i_{id} + \omega L_f i_{iq} \\ L_f \frac{di_{iq}}{dt} = u_{iq} - u_{oq} - R_f i_{iq} + \omega L_f i_{id} \\ C_f \frac{du_{od}}{dt} = i_{id} - i_{od} + \omega C_f u_{oq} \\ C_f \frac{du_{oq}}{dt} = i_{iq} - i_{oq} + \omega C_f u_{od} \\ L \frac{di_{od}}{dt} = u_{od} - u_{cd} - R i_{od} + \omega L i_{oq} \\ L \frac{di_{oq}}{dt} = u_{oq} - u_{cq} - R i_{oq} + \omega L i_{od} \end{cases} \quad (24)$$

R_f is for damping resistor for the filter oscillation suppression, R, L is the line resistance and inductance. u_{cd}, u_{cq} are microgrid AC bus voltage d, q-axis component.

We use microgrid initial steady state operating point angular frequency ω_o to linearise the formula (24) to get the output filter and the network small signal state-space model:

$$\begin{bmatrix} \Delta \dot{i}_{idq} \\ \Delta u_{odq} \\ \Delta \dot{i}_{odq} \end{bmatrix} = A_{LW} \begin{bmatrix} \Delta i_{idq} \\ \Delta u_{odq} \\ \Delta i_{odq} \end{bmatrix} + B_{LW} \Delta u_{idq} + C_{LW} \Delta u_{cdq} + D_{LW} \Delta \omega \quad (25)$$

Wherein the coefficient matrix are

$$A_{LW} = \begin{bmatrix} \frac{R_f}{L_f} & \omega_o & -\frac{1}{L_f} & 0 & 0 & 0 \\ -\omega_o & \frac{R_f}{L_f} & 0 & -\frac{1}{L_f} & 0 & 0 \\ \frac{1}{C_f} & 0 & 0 & \omega_o & -\frac{1}{C_f} & 0 \\ 0 & \frac{1}{C_f} & -\omega_o & 0 & 0 & -\frac{1}{C_f} \\ 0 & 0 & \frac{1}{L} & 0 & -\frac{R}{L} & \omega_o \\ 0 & 0 & 0 & \frac{1}{L} & -\omega_o & -\frac{R}{L} \end{bmatrix}, \quad B_{LW} = \begin{bmatrix} \frac{1}{L_f} & 0 \\ 0 & \frac{1}{L_f} \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}, \quad C_{LW} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ -\frac{1}{L} & 0 \\ 0 & -\frac{1}{L} \end{bmatrix}, \quad D_{LW} = \begin{bmatrix} I_{iq} & -I_{id} & U_{oq} & -U_{od} & I_{oq} & -I_{od} \end{bmatrix}^T$$

4.2.4 Inverter Power Parallel System Small Signal Model

All the above portions small signal model are established under the rotating coordinate system determined by inverter power output voltage. In order to establish the entire micro-grid system small-signal model, these models need to be converted to the common reference coordinate system.

According to coordinate transformation method described above, inverter power output current converted to the common reference coordinate system is:

$$i_{oDQ} = T i_{odq} = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} i_{odq} \quad (26)$$

Linearize formula (26) can get

$$i_{oDQ} = T i_{odq} = T_i \Delta \theta \quad (27)$$

Wherein the T_i is matrix contains two elements. Its expression is

$$T_i = \begin{bmatrix} -I_{od} \sin \theta - I_{oq} \cos \theta \\ I_{od} \cos \theta - I_{oq} \sin \theta \end{bmatrix}$$

Microgrid AC bus voltage is a variable in the common reference coordinate system. It can convert to the inverter itself rotating coordinate system using coordinate inverse transformation formula.

$$u_{cdq} = T^{-1} u_{CDQ} = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix} u_{CDQ} \quad (28)$$

Linearize formula (28) can get

$$\Delta u_{cdq} = T^{-1} u_{CDQ} + T_u^{-1} \Delta \theta \quad (29)$$

$$T_u^{-1} = \begin{bmatrix} -U_{CD} \sin \theta + U_{CQ} \cos \theta \\ -U_{CD} \cos \theta - U_{CQ} \sin \theta \end{bmatrix}$$

Wherein

By considering the formulas(8)-(29), we can obtain inverter power x small signal state-space model:

$$\begin{cases} \Delta \dot{x}_{invx} = A_{invx} \Delta x_{invx} + B_{invx} \Delta u_{CDQ} + B_{x\omega_{com}} \Delta \omega_{com} \\ \begin{bmatrix} \Delta \omega_x \\ \Delta i_{oDQx} \end{bmatrix} = \begin{bmatrix} C_{inv\omega x} \\ C_{invx} \end{bmatrix} \Delta x_{invx} \end{cases} \quad (30)$$

$\Delta x_{invx} = [\Delta \theta_x \quad \Delta P_x \quad \Delta Q_x \quad \Delta \psi_{dqx} \quad \Delta \lambda_{dqx} \quad \Delta i_{idqx} \quad \Delta u_{odqx} \quad \Delta i_{odqx}]^T$, the coefficient matrix are

$$A_{invx} = \begin{bmatrix} A_{p(3 \times 3)} & 0_{3 \times 2} & 0_{3 \times 2} & B_{p(3 \times 6)} \\ (B_{u1} C_{pu})_{2 \times 3} & 0_{2 \times 2} & 0_{2 \times 2} & B_{u2(2 \times 6)} \\ (B_{i1} D_{u1} C_{pu})_{2 \times 3} & (B_{i1} C_u)_{2 \times 2} & 0_{2 \times 2} & (B_{i1} D_{u2} + B_{i2})_{2 \times 6} \\ \left\{ \begin{array}{l} B_{LW} D_{i1} D_{u1} C_{pu} + \\ C_{LW} [T_u^{-1} \quad 0_{2 \times 1} \quad 0_{2 \times 1}] \\ + D_{LW} C_{pu} \end{array} \right\}_{6 \times 3} & (B_{LW} D_{i1} C_u)_{6 \times 2} & (B_{LW} C_i)_{6 \times 2} & \left(\begin{array}{l} A_{LW} + B_{LW} D_{i1} D_{u2} \\ + B_{LW} D_{i2} \end{array} \right)_{6 \times 6} \end{bmatrix} \quad \text{J13413}$$

$$B_{invx} = \begin{bmatrix} 0_{3 \times 2} \\ 0_{2 \times 2} \\ 0_{2 \times 2} \\ (C_{LW} T^{-1})_{6 \times 2} \end{bmatrix}_{13 \times 2}, \quad B_{x\omega_{com}} = \begin{bmatrix} (B_{p\omega})_{3 \times 1} \\ 0_{2 \times 1} \\ 0_{2 \times 1} \\ 0_{6 \times 1} \end{bmatrix}_{13 \times 1}$$

$$C_{inv\omega x} = \begin{bmatrix} (X_{p\omega})_{1 \times 3} & 0_{1 \times 2} & 0_{1 \times 2} & 0_{1 \times 6} \end{bmatrix}_{1 \times 13}$$

$$C_{invx} = \begin{bmatrix} [T_{12 \times 1} & 0_{2 \times 1} & 0_{2 \times 1}]_{2 \times 3} & 0_{2 \times 2} & 0_{2 \times 2} & [0_{2 \times 2} & 0_{2 \times 2} & T_{2 \times 2}]_{2 \times 6} \end{bmatrix}_{2 \times 13}$$

In this paper, micro-grid system contains two inverter power . Usually the first inverter rotating coordinate system is as a common reference coordinate system, thus

$$X_{p\omega} = \begin{cases} \begin{bmatrix} 0 & -m_p & 0 \end{bmatrix} & x=1 \\ \begin{bmatrix} 0 & 0 & 0 \end{bmatrix} & x \neq 1 \end{cases}$$

In sum, two inverters parallel system small signal state space model is:

$$\begin{cases} \begin{bmatrix} \dot{\Delta x}_{inv1} \\ \Delta x_{inv1} \\ \dot{\Delta x}_{inv2} \\ \Delta x_{inv2} \end{bmatrix} = A_{inv} \begin{bmatrix} \Delta x_{inv1} \\ \Delta x_{inv2} \end{bmatrix} + B_{inv} \Delta u_{CDQ} \\ \Delta i_{oDQ} = C_{inv} \begin{bmatrix} \Delta x_{inv1} \\ \Delta x_{inv2} \end{bmatrix} \end{cases} \quad (31)$$

The coefficient matrix formulas are as follows:

$$A_{inv} = \begin{bmatrix} (A_{inv1} + B_{1\omega_{com}} C_{inv\omega1})_{13 \times 13} & 0_{13 \times 13} \\ (B_{2\omega_{com}} C_{inv\omega1})_{13 \times 13} & A_{inv2} \end{bmatrix}_{26 \times 26}$$

$$B_{inv} = \begin{bmatrix} B_{inv1} \\ B_{inv2} \end{bmatrix}_{26 \times 2}, \quad C_{inv} = \begin{bmatrix} C_{invc1} & 0_{2 \times 13} \\ 0_{2 \times 13} & C_{invc2} \end{bmatrix}_{4 \times 26}$$

4.3 Load small-signal model

load current i_{load} meets the following differential algebra equation:

$$\begin{cases} L_{load} \frac{di_{loadD}}{dt} = u_{CD} - R_{load} i_{loadD} + \omega L_{load} i_{loadQ} \\ L_{load} \frac{di_{loadQ}}{dt} = u_{CQ} - R_{load} i_{loadQ} - \omega L_{load} i_{loadD} \end{cases} \quad (32)$$

Formula (32) were linearized small signal load available state-space model:

$$\Delta i_{loadDQ} = A_{Load} \Delta i_{loadDQ} + B_{Load1} \Delta u_{CDQ} + B_{Load2} \Delta \omega \quad (33)$$

Wherein the coefficient matrices are

$$A_{Load} = \begin{bmatrix} -\frac{R_{load}}{L_{load}} & \omega_o \\ \omega_o & -\frac{R_{load}}{L_{load}} \end{bmatrix}, \quad B_{Load1} = \begin{bmatrix} \frac{1}{L_{load}} & 0 \\ 0 & \frac{1}{L_{load}} \end{bmatrix}, \quad B_{Load2} = \begin{bmatrix} I_{loadQ} \\ -I_{loadD} \end{bmatrix}$$

4.4 micro-grid small-signal model

From(31)and (33) , it can be seen that micro-grid AC bus voltage is input variables for each sub-

model, and through micro-grid AC bus voltage , each subsystem can be combined to form a complete micro-grid small-signal state space model.

In order to better determine the micro-grid AC bus voltage , We assume that r_n is the exchange for micro-grid AC bus virtual resistance to ground. In order to reduce the impact on system dynamic stability, r_n general should choose a larger value, here $3 \times 10^7 \Omega$.

Therefore, micro-grid AC bus voltage can be expressed as

$$u_{CD} = r_n (i_{oD1} + i_{oD2} - i_{loadD}) \quad (34)$$

$$u_{CQ} = r_n (i_{oD1} + i_{oD2} - i_{loadQ}) \quad (35)$$

Formula (34) and (35) can be linearized to get

$$\Delta u_{CDQ} = R_N M_{inv} \Delta i_{oDQ} + R_N M_{load} \Delta i_{loadDQ} \quad (36)$$

The coefficient matrix formulas are as follows:

$$R_N = \begin{bmatrix} r_n & 0 \\ 0 & r_n \end{bmatrix}, \quad M_{inv} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}, \quad M_{load} = \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix}$$

By considering the formulas(31)(33)(36),and eliminating intermediate variables, we can get microgrid system complete small-signal state space model:

$$\begin{bmatrix} \dot{\Delta x}_{inv} \\ \Delta i_{loadDQ} \end{bmatrix} = A_{mg} \begin{bmatrix} \Delta x_{inv} \\ \Delta i_{loadDQ} \end{bmatrix} \quad (37)$$

Wherein $\Delta x_{inv} = [\Delta x_{inv1} \quad \Delta x_{inv2}]^T$,the coefficient matrices are

$$A_{mg} = \begin{bmatrix} (A_{inv} + B_{inv} R_N M_{inv} C_{inv})_{26 \times 26} & (B_{inv} R_N M_{load})_{26 \times 2} \\ (B_{Load1} R_N M_{inv} C_{inv} + B_{Load2} C_{inv\omega})_{2 \times 26} & (A_{inv} + B_{Load1} R_N M_{load})_{2 \times 2} \end{bmatrix}_{28 \times 28}$$

$$C_{inv\omega} = [C_{inv\omega1} \quad C_{inv\omega2}]_{1 \times 26}$$

4.5 different parameters affect the stability analysis

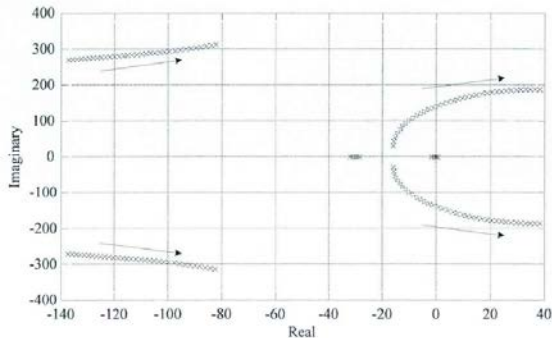
As we already established a microgrid islands small-signal state space model , eigenvalue analysis of its state matrix is an important means to determine the micro-grid stability, but also of change of different parameters such as active and reactive droop factor, line parameters effect on the stability.

Table 1 Islands microgrid stable operating parameters

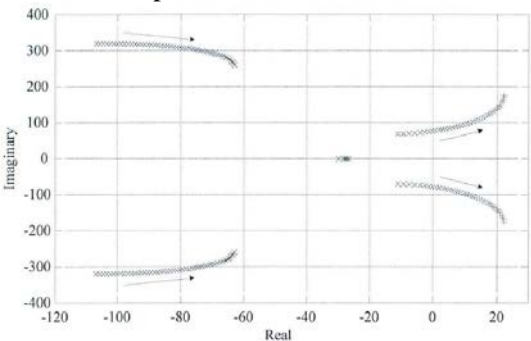
Parameters (Value)	Parameters (Value)	Parameters (Value)	Parameters (Value)
U_{od} [311.2 311.2]	U_{oq} [0 0]	I_{od} [3.3 3.3]	I_{oq} [0.4 1.2]

$$\begin{array}{cccc}
 I_{ld} & [3.5 & I_{lq} & [1.5 & U_{CD} [310.8] & U_{CQ} [0 \\
 3.5] & & 2.3] & & & \\
 I_{loadD} [6.6] & I_{loadQ} [5] & \omega_o [314] & \theta 1.8^\circ & &
 \end{array}$$

Put the system parameters and initial steady state operating parameters into the established micro-grid small-signal state space model coefficient matrix, using Matlab software program to calculate and plot the trajectory of the eigenvalues of the state matrix with the parameters change, in order to determine the system stability.



(a) Eigenvalues change trajectory when active droop coefficient m increases



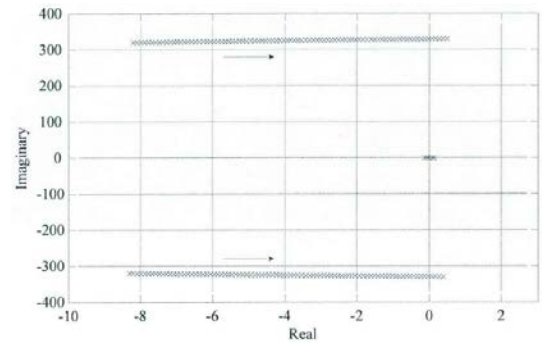
(b) eigenvalues trajectory when reactive droop variation coefficient n increases

Figure 16 eigenvalues trajectory when active and reactive droop coefficient changes

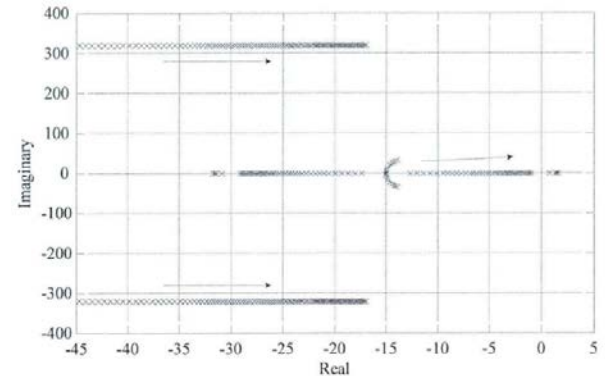
1) active and reactive power droop characteristic coefficient influence on the stability

When active droop coefficient m from 1×10^{-5} increases to 1×10^{-3} , reactive droop factor n increases from 3×10^{-4} increases to 3×10^{-2} , the most near to the imaginary axis eigenvalues trajectory are shown in Figure 16 (a), (b).

As can be seen from Figure 16, with the active and reactive droop coefficient increases, the eigenvalues are gradually close to the imaginary axis, even to the positive real part, so the droop coefficient increases will reduce the microgrid system stability.



(a)eigenvalues trajectory when reduce the line resistance



(b)eigenvalues trajectory when reduce the line inductance

Figure 17 eigenvalues trajectory when the line impedance parameters change

2) line impedance parameters affect the stability

When the line resistance $R_{l(2)}$ reduces from 0.1282Ω to 0.000641Ω , the inductance $L_{l(2)}$ reduce from $64.3\mu H$ to $0.64\mu H$, as can be seen from the figure, with the line resistance or inductance decreases, eigenvalues are closer to the imaginary axis even to positive real part, thus reducing the line impedance will reduce the stability of the micro-grid system.

4.6 Stability simulation

We use simulation tools to further study the active, reactive droop factor and line parameters affect the stability of the micro-grid system.

Study 1: other conditions remain unchanged, only when the active droop coefficient m from the initial steady-state operation 1×10^{-5} to increase to 5×10^{-4} . The inverter power output power and system frequency response curve are shown in Figure 18.

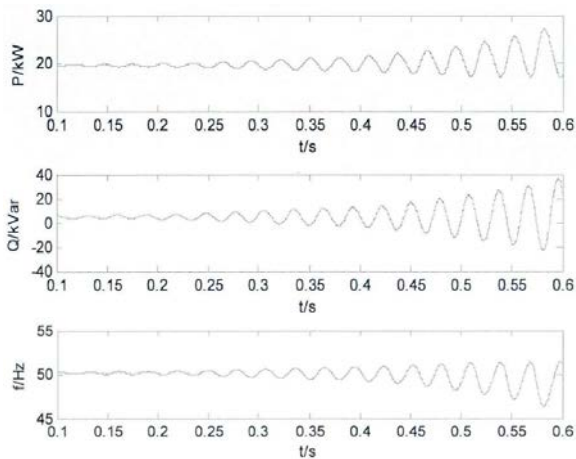


Figure 18 simulation waveforms of active droop coefficients $m = 5 \times 10^{-4}$

As can be seen from Figure 18, when the active droop coefficient m is larger, inverter power output active and reactive power and system frequency will produce oscillation, micro-grid system becoming unstable.

Example 2: other conditions remain unchanged, only when the reactive droop coefficient n increases from the initial steady-state operation 3×10^{-4} to 3×10^{-3} , inverter power 1 output power and micro-grid AC bus voltage response curve are shown in Figure 19. As we can be seen from the figure, when n is larger, the inverter output active and reactive power fluctuation is larger, and deviates from the initial steady-state operation value. Microgrid AC bus voltage amplitude drop magnitude is beyond the initial steady-state operating voltage amplitude fluctuations allowed taxis 5% range. Therefore, when the reactive droop factor n increases, the micro-grid system is easy to lose stability.

Operation example 3: other conditions remain unchanged, when the line impedance parameters from the initial steady-state operation $R_{l(2)} = 0.1282\Omega$, $L_{l(2)} = 64.3\mu H$ reduced to $R_{l(2)} = 0.016025\Omega$, $L_{l(2)} = 8.0375\mu H$, the inverter power 1 output power and system frequency response curve are shown in Figure 20. As we can be seen from the figure, when the line impedance parameters is smaller, inverter power output active power, reactive power and system frequency will produce oscillation. And micro-grid system will lose stability.

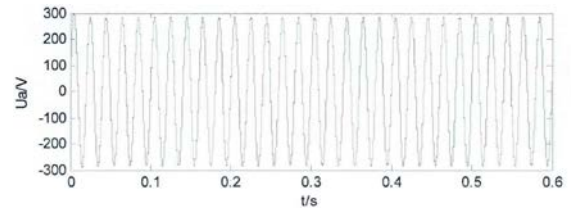
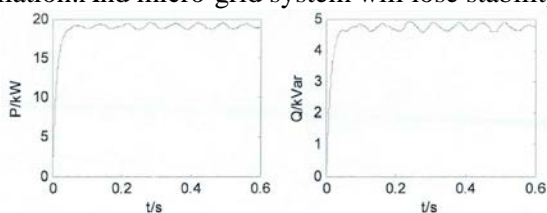


Figure 19 The reactive droop coefficient $n = 3 \times 10^{-3}$ simulation waveforms

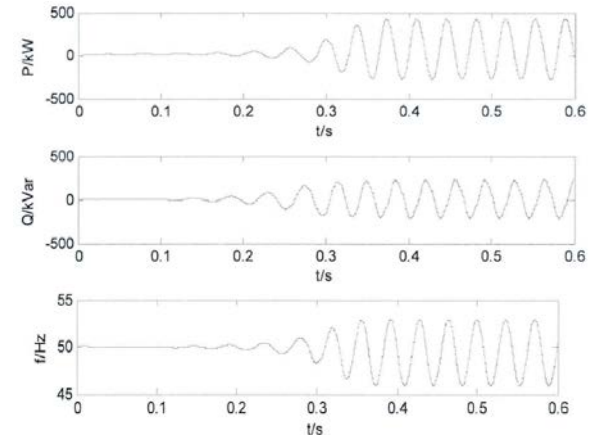


Figure 20 line impedance parameters $R_{l(2)} = 0.016025\Omega$, $L_{l(2)} = 8.0375\mu H$ simulation waveform

Simulation results show that the micro-grids small signal stability analysis related conclusions are correct. We can use these results to take appropriate measures to enhance the stability of the micro-grid system. For example when the line impedance is small, we can string into proper little resistance and inductance, droop coefficient, etc.

5 Conclusion and Outlook

5.1 Conclusion and Summary

Microgrid based on droop control can achieve automatically adjust voltage and frequency, without the aid of communication, which can improve system reliability, and easy to implement micro-power and load plug and play. This article describes the micro-grid inverter study background and significance. The working principle of micro-grid droop control method is studied and built their model circuit diagram on psim software. After simulation operation, the output waveforms show that the control strategy designed can stabilize the output power, and satisfy the system requirements of voltage amplitude and frequency. That proves the correctness of such a microgrid control strategy. It has established an island microgrid complete small-signal state space model, which took into account

the inverter power small-signal sub-model, network lines and the load small signal sub-model. Use eigenvalue method to analysis microgrid small signal model state matrix, to get the following conclusions: droop coefficient increases will reduce the stability of the micro-grid system; when the line impedance is smaller, micro-grid is easy to lose stability. Finally, We use the simulation tools to verify the small signal stability analysis conclusions is correct.

5.2 Prospects

Due to time constraints, as well as lack of practical experience, this article only do a little preliminary researchs on micro-grid inverter control this broad field, which will inevitably be some flaws. We also need to do more research in the following areas and learning:

1) DC side uses a DC voltage source, in less ideal circumstances, the distributed power situation is very complex. There are intermittent and persistent type of distributed power generation division.

2) This article is aimed at small perturbation to analyze the stability of the micro-grid. It need further study on micro-grid system transient stability dealing with large disturbances.

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